

Proposal of a New Block Cipher reasonably Non-Vulnerable against Cryptanalytic Attacks

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Abstract

This paper proposes a new block cipher termed as “Modular Arithmetic based Block Cipher with Varying Key-Spaces (MABCVK)” that uses private key-spaces of varying lengths to encrypt data files. There is a simple but intelligent use of theory of modular arithmetic in the scheme of the cipher. Based on observed implementation of the proposed cipher on a set of real data files of several types, all results are tabulated and analyzed. The schematic strength of the cipher and the freedom of using a long key-space expectedly can make it reasonably non-vulnerable against possible cryptanalytic attacks. As a part of the future scope of the work, it is also intended to formulate and implement an enhanced scheme that will use a carrier image to have a secure transmission of the private key

Keywords: *Cryptography, Modular Arithmetic, Carrier Image, Data Security*

1. Introduction

Module arithmetic [1], a strong backbone in numerous existing ciphering protocols [2], has been applied in an intelligent manner to develop “Modular Arithmetic based Block Cipher with Varying Key-Spaces” with the acronym as MABCVK. Although the encryption of data using MABCVK results in encrypted data of extended dimension, its schematic strength and the liberty of using a long key-space while encrypting using it expectedly can make MABCVK reasonably non-vulnerable against possible cryptanalytic attacks.

Section 2 presents the scheme followed in MABCVK. A report of implementation of MABCVK on a sample plaintext is demonstrated in section 3. Results of a set of real implementations are presented in section 4. Section 5 is an analytical observation to MABCVK. A conclusion is drawn in section 6.

2. The Scheme

The data to be encrypted is divided in blocks each of L -bits. All these blocks are converted into equivalent set of integers of base-10. Next, two sufficiently large prime integers K_1 and K_2 are taken as keys satisfying the conditions:

1. K_1, K_2 being sufficiently bigger than the number or numbers to be encrypted
2. $K_1 < K_2$

A variable α with its value being in the range of 0.1 and 0.9 is taken to be used in due course of time to shift the sequence of encrypted set of integers. Sections 2.1 and section 2.2 respectively describe the encryption and the decryption processes with conventionally *Alice* being considered as the sender and *Bob* being considered as the receiver

2.1 Encryption

The set of computations to be done in the encryption end for P being a positive integer to be encrypted is as follows:

1. Set $K_3 = \phi(K_1) - 1$.
2. Set A = Chosen random number from the set of numbers, which when used as quotient to divide K_2 , leaves P as remainder.
3. Set $B = A^{K_3} \text{ mod } K_1$
4. Set C = Product of B and K_2

5. Set $D = C^{K3} \text{ mod } K1$
6. Set $E = \text{Result of shifting } D \text{ by } \alpha \%$, which is the encrypted form for P.

The function $\phi(K1)$ is a totient function [3]. The totient $\phi(K1)$ of a positive integer $K1$ defines the number of integers less than or equal to $K1$ that are relatively prime to $K1$. $\phi(K1) = K1 - 1$, when $K1$ is a prime number.

2.2 Decryption

Based on the set of values for $K1, K2, \alpha$ extracted from the private key, the following set of operations are carried out in the decryption end.

1. Set $K3 = \phi(K1) - 1$.
2. Set $D = \text{Result of shifting } E \text{ by } (1 - \alpha)\%$
3. Set $B = (D \cdot K2)^{K3} \text{ mod } K1$
4. Set $A = B^{K3} \text{ mod } K1$
5. Set $P = K2 \text{ mod } A$

The function $\phi(K1)$ is a totient function as was described in section 2.1.

3. Implementation

This section describes the process of encryption and decryption using a sample tiny plaintext WORLD considering $K1 = 263, K2 = 317$ and $\alpha = 0.1$.

Table 1 enlists different intermediate and the final result of implementation following the encryption algorithm stated in section 2.1. Consequently, the cipher text “U≤a¼E” is generated for the taken plaintext

Character	Value obtained by following step 2 of the Encryption Algorithm	Value obtained by following step 3 of the Encryption Algorithm	Value obtained by following step 4 of the Encryption Algorithm	Value obtained by following step 5 of the Encryption Algorithm	Character corresponding to value obtained through step 5 of the Encryption Algorithm	Character obtained by following step 6 of the Encryption Algorithm for an assumed value of 0.1 for α
W	87	230	255	80835	14	E
O	79	119	42	13314	85	≤
R	82	235	216	68472	243	a
L	76	241	251	79567	97	¼
D	68	83	244	77348	172	E

A reverse process is followed to employ the decryption algorithm stated in section 2.2.

4. Results

The implementation of the encryption / decryption algorithm described in section 2.1 and section 2.2

respectively was accomplished using C language and MIRACL (Multi precision Integer and Rational Arithmetic C/C++ Library) library [4] for big integer calculations. The plaintext to be encrypted was read as blocks of 8-bits, a pair of private keys KEY1 and KEY2, each 10-bits long, and a small value α was taken for operation on the plaintext data.

Ciphertext data produced after encryption process was written as blocks of 32-bits i.e. size of integer type variable, to avoid overflow, as in some cases 8-bit data after encryption is to yield a value greater than 255. We have encrypted and also successfully decrypted file types .txt, .doc, .docx, .xls, .pdf, .mp4, .ocx, .jpg, .bmp, .dll, .gif, .sys etc.

A comparison of file type, source file size, decrypted file size, encryption time and decryption time is depicted in the table 2.

It is seen from data in Table 2 that the relation between encryption time and file size is linear. The average time, based on tabulated data in table 2, to encrypt 1 KB of data is remarkably found to be 0.028852538 seconds. Similarly, it was noted that the average time required for decryption of 1 KB of data is 0.007198586 seconds.

Each 8-bit source data is written as 32-bit encrypted data, so the encrypted data file size (in bytes) is approximately four times the source data file size (in bytes). Thus it was observed that the proposed cipher carries a schematic overhead of causing data expansion. Having computational complexities, an operational overhead of being marginally slow in execution is observed during its real implementation.

sl no	Source filename	size (in kb)	encryption time (sec)	Encrypted file size (in KB)	Encrypted filename	Decryption Time (sec)	Decrypted File size (in KB)
1	abc.docx	47	1.516	188	abc.docx.enc	1.5	47
2	hawaii.jpg	18	0.64	71	hawaii.jpg.enc	0.656	18
3	3rd sem2011.docx	47	1.532	188	3rd sem2011.docx.enc	1.5	47
4	cv.doc	60	1.219	238	cv.doc.enc	1.235	60
5	EffectCtrl.ocx	405	11.203	1617	EffectCtrl.ocx.enc	11.172	405
6	Flower.bmp	17	0.625	68	Flower.bmp.enc	0.625	17
7	hummapl.dll	59	1.532	236	hummapl.dll.enc	1.516	59
8	internal marks.xls	85	1.781	338	internal marks.xls.enc	1.719	85
9	Crypto.zip	66	2.172	261	Crypto.zip.enc	2.188	66
10	test.txt	2	0.125	7	test.txt.enc	0.11	2
11	Univ tabulator.pdf	434	13.625	1736	Univ tabulator.pdf.enc	13.688	434
12	Vivekananda.gif	25	0.875	100	Vivekananda.gif.enc	0.875	25
13	BuzzingBee.wav	144	4.829	573	BuzzingBee.wav.enc	4.765	144
14	clock.avi	81	2.578	324	clock.avi.enc	2.484	81
15	EffectCtrl.ocx	405	11.219	1617	EffectCtrl.ocx.enc	11.266	405
16	Gone Fishing.bmp	17	0.625	68	Gone Fishing.bmp.enc	0.641	17
17	Greenstone.bmp	26	0.875	104	Greenstone.bmp.enc	0.844	26
18	handsafe.reg	1	0.031	3	handsafe.reg.enc	0.031	1
19	himem.sys	5	0.234	19	himem.sys.enc	0.234	5
20	IE7/Enla.rtf	73	2.469	292	IE7/Enla.rtf.enc	2.485	73
21	rvview.exe	151	3.156	602	rvview.exe.enc	3.14	151
22	Keyboard.drv	2	0.094	8	Keyboard.drv.enc	0.109	2
23	Mscomm32.ocx	102	2.828	406	Mscomm32.ocx.enc	2.765	102
24	normafd.nls	39	1.063	154	normafd.nls.enc	1.031	39
25	notepad.exe	68	1.797	270	notepad.exe.enc	1.734	68
26	PreConvertLite.dll	103	2.969	412	PreConvertLite.dll.enc	2.953	103

Figure 1 shows plotting of source file size (in KB) and encryption time (in Sec).

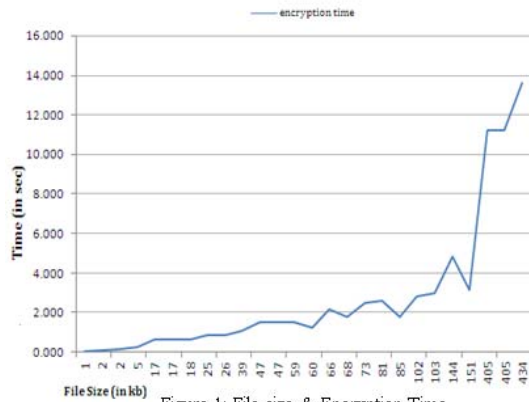


Figure 1: File size & Encryption Time

Figure 2 shows plotting of file size and decryption time.

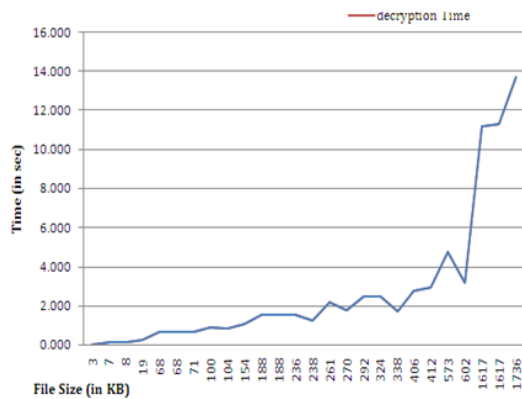


Figure 2: File size & Decryption Time

The encryption and decryption process being almost symmetrical, the encryption time for any specific file is nearly equal to the time required to decrypt it. This is validated from the graph plotting shown in figure 1 and figure 2.

5. Analysis

Although small keys were used to tabulate results of encryption using MABCVK, it can be used with much larger key-spaces with the support of appropriate computing platform for large exponential computations.

The substitution of plaintext data with random integers generates different ciphers for the same set of keys. If the number of integers to be encrypted is N and if there can be at least one substitution for each then there can be at least N different cipher texts generated using the same key sets. This property makes frequency analysis attacks difficult.

The effective key length is equal to sum of length of KEY1 and KEY2. Brute-force search will require searching entire search space of $2^{(\text{sum of length of KEY1 \& KEY2})}$.

The average time required for such extensive search is given in table 3 [5].

Key Size(Bits)	Number of Alternative Keys	Time Required at 1 Encryption / μ s	Time Required at 10^6 encryptions / μ s
56	$2^{56} = 7.2 \times 10^{16}$	$2^{56} \mu$ s = 1142 years	10.01 hours
128	$2^{128} = 3.4 \times 10^{38}$	$2^{127} \mu$ s = 5.4×10^{24} years	5.4×10^{18} years
168	$2^{168} = 3.7 \times 10^{50}$	$2^{167} \mu$ s = 5.9×10^{36} years	5.9×10^{30} years
26 characters	$26! = 4 \times 10^{26}$	$2 \times 10^{26} \mu$ s = 6.4×10^{12} years	6.4×10^6 years

Data expansion noted during encryption is expected as the proposed cipher uses exponentiation. We can adopt to write encrypted data as bit stream and devise an appropriate padding scheme to identify separate blocks to reduce the encrypted file size considerably. The computational complexity of calculating large integer powers of integers can be simplified by adopting faster methods like exponentiation by squaring, square and multiply or binary exponentiation, which leads to reduction of both encryption and decryption time. Encryption process can be augmented to be faster if read block size (in bits) is increased but it should be less than the size of key (in bits). The proposed scheme restricts use of the read block size greater than the key size.

6. Conclusion

The proposed MABCVK is flexible enough for implementation with larger keys. The substitution of source data with random integers produces different sets of encrypted data for the same private key pairs, which, in turn, makes the task of cryptanalysis a challenging one. Encryption and decryption using MABCVK require almost same execution time. If a pair of 128-bit keys is used for encryption and if brute-force attack is applied for decryption then at least all the primes in the range of integers from 1 to 2^{128} are to be tested as a probable key. There are $2^{128} / \text{Log}(2^{128}) = 383534127545935 \times 10^{22}$ prime numbers in the range of integers from 1 to 2^{128} . It is observed that if one trillion of these numbers per second can be checked, more than $121,617,874,031,562 \times 10^3$ years is required to check all such primes. The requirement of time as shown in table 3, to calculate the keys makes it reasonably non-vulnerable against cryptanalytic attacks. As a part of the future scope of the work, it is also intended to formulate and implement an enhanced scheme that will use a carrier image to have a secure transmission of the private keys.

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